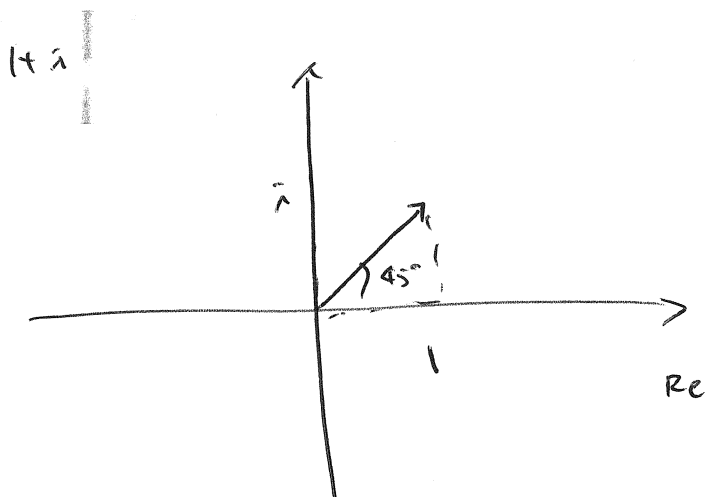
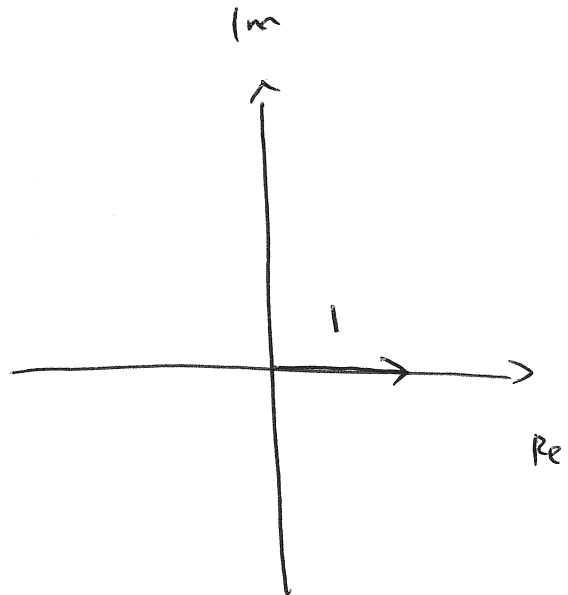
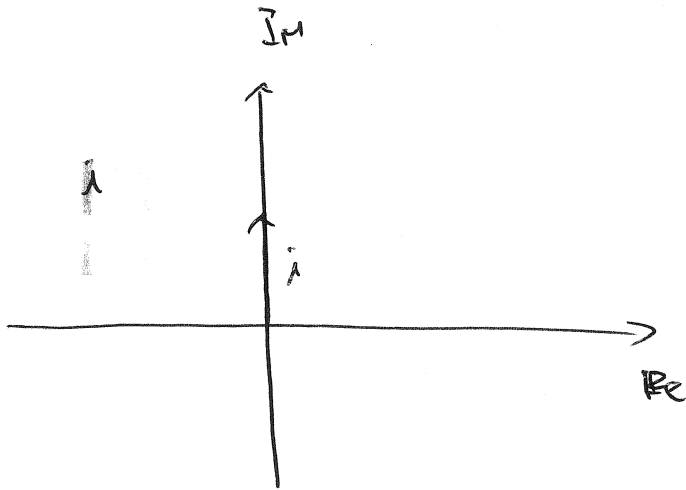
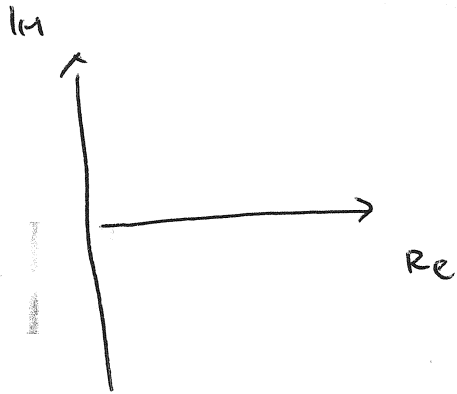
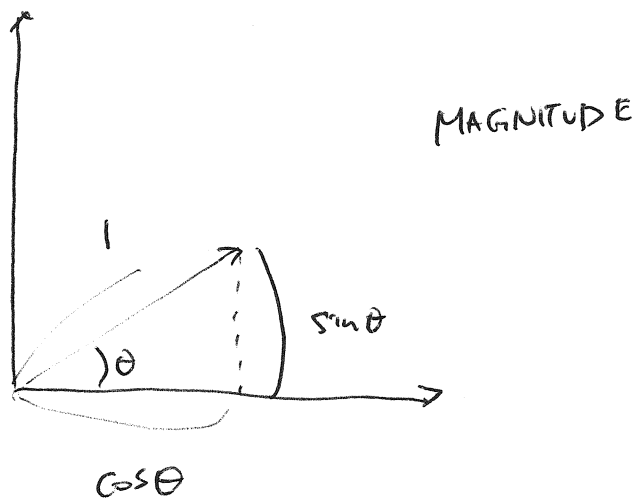


WHY'S BORED W/ PHYSICS?
COMPLEX NUMBERS INTEREST

$$i = \sqrt{-1}$$





$$\cos \theta + i \sin \theta$$

↓

EULER RELATIONS

COINCIDER?

$e^{-i\pi/2}$
e

a. $1 - i$

b. $1 + i$

c. $\frac{1}{\sqrt{2}} + \frac{i}{\sqrt{2}}$

d. $\frac{1}{\sqrt{2}} - \frac{i}{\sqrt{2}}$

EULER RELATIONSHIP

$$e^{i\theta} = \cos\theta + i\sin\theta$$

$$e^{-i\theta} = \cos\theta - i\sin\theta$$

$$\cos\omega t = \operatorname{Re} e^{i\omega t}$$

EXAMPLE

~~$V(t) = V_m \cos\omega t$~~ $V(t) = V_m \cos\omega t = \operatorname{Re} e^{i\omega t}$

$$I(t) = I_m \cos(\omega t - \phi) = \operatorname{Re} e^{i(\omega t - \phi)}$$

$$\frac{V(t)}{I(t)} = R? = \frac{V_m e^{i\omega t}}{I_m e^{i(\omega t - \phi)}} = \frac{V_m}{I_m} e^{i\phi}$$



O.K. TRY THIS

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$$V(t) = V_m e^{i\omega t}$$

$$V(t) - L \frac{dI}{dt} = 0$$

$$V_m e^{i\omega t} - L \frac{dI}{dt} = 0$$

$$V_m e^{i\omega t} = L \frac{dI}{dt}$$

$$\frac{dI}{dt} = \frac{V_m}{L} e^{i\omega t}$$

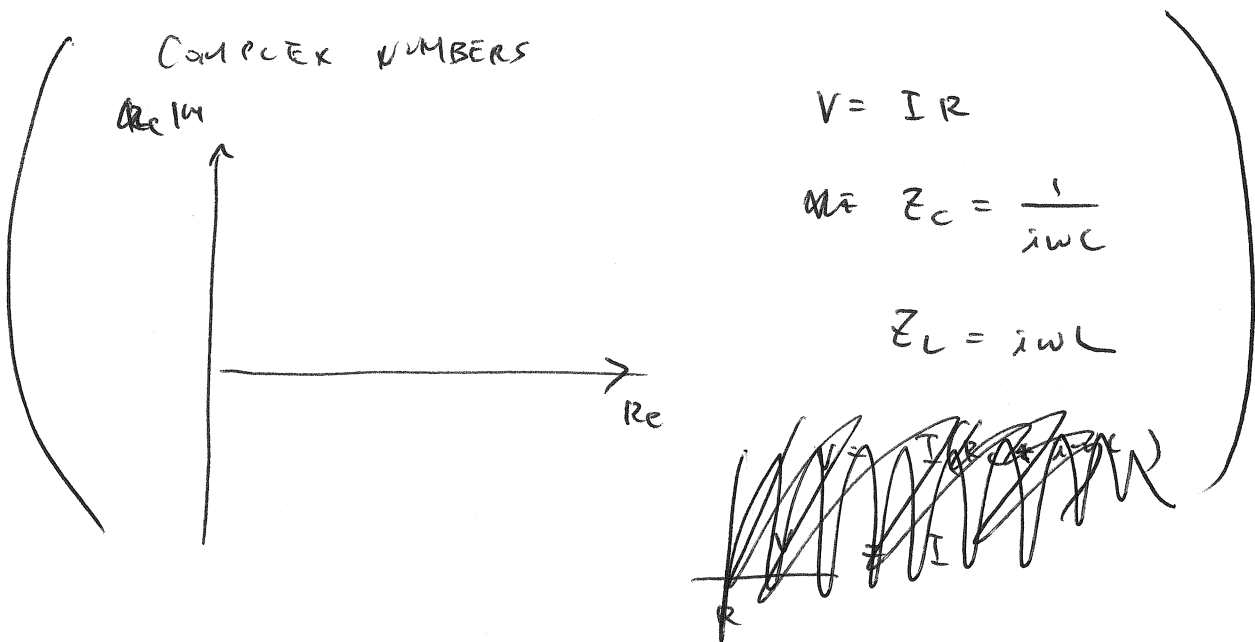
$$I(t) = \frac{V_m}{i\omega L} e^{i\omega t}$$

$$I(t) = \frac{-i V_m}{\omega L} e^{i\omega t}$$

$$-i = e^{-i\pi/2}$$

$$I(t) = \frac{V_m}{\omega L} e^{i(\omega t - \pi/2)}$$

LAGS!



COMPLEX IMPEDANCE

$$I(t) = \frac{V_m}{i\omega L} e^{i\omega t}$$

$$I(t) = \frac{V(t)}{i\omega L}$$

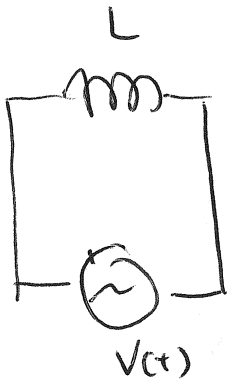
$$V(t) = I(t) i\omega L$$

$$V(t) = I(t) Z_L$$

$$Z_L = i\omega L$$

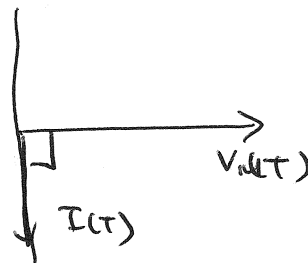
$$Z_C = \frac{1}{i\omega C}$$

How do I USE IT?

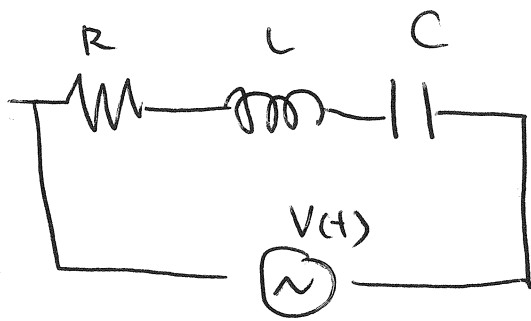


$$V(t) = I(t) i\omega L$$

$$I(t) = \frac{V(t)}{i\omega L} = -i \frac{V(t)}{\omega L}$$



90° LAGGING!



$$Z_{\text{TOTAL}} = R + i\omega L + \frac{1}{i\omega C}$$

$$= R + i\left(\omega L - \frac{1}{\omega C}\right)$$

$$|Z_{\text{TOTAL}}| = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

$$I(t) = \frac{V_m(t)}{Z_{\text{TOTAL}}}$$

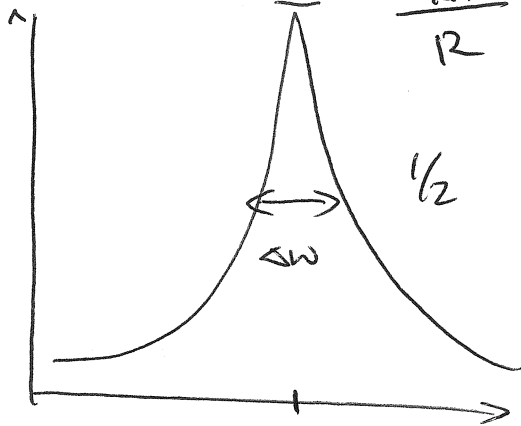
$$= \frac{V_m(t)}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}} \frac{R - i\left(\omega L - \frac{1}{\omega C}\right)}{\left[R + i\left(\omega L - \frac{1}{\omega C}\right)\right] \left[R - i\left(\omega L - \frac{1}{\omega C}\right)\right]}$$

$$= \frac{V_m(t)}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}} \frac{R - i\left(\omega L - \frac{1}{\omega C}\right)}{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

$$I(t) = \frac{V_m}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}} e^{i(\omega t - \phi)}$$

$$\phi = \tan^{-1} \frac{\left(\omega L - \frac{1}{\omega C}\right)}{R}$$

Power



$$\omega = \frac{1}{\sqrt{LC}}$$

$$P(t) = I_m V_m \left[\cos^2 \omega t \cos \phi + \sin(2\omega t) \sin \phi \right]$$

$$P_{\text{AVERAGE}} = I_m V_m \frac{1}{2} \cos \phi$$

$$P_{\text{AVE}} = \frac{I_m V_m}{\sqrt{2} \sqrt{2}} \frac{V_m^2}{|Z|} \frac{1}{2} \cos \phi = \frac{1}{|Z|} V_{\text{RMS}}^2 \cos \phi$$

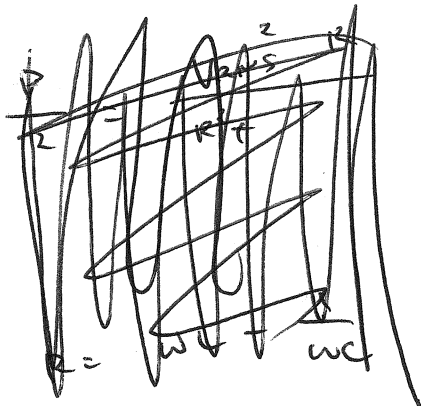
$\cos \phi$ POWER FACTOR

RLC CIRCUIT

$$P_{\text{AVERAGE}} = \frac{1}{|Z|} V_{\text{RMS}}^2 \cos \phi$$

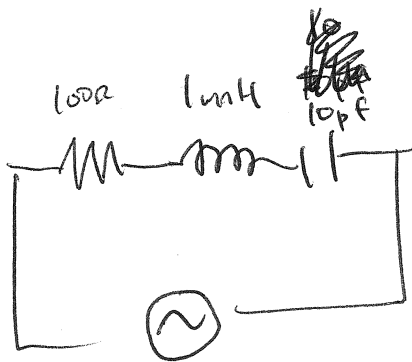
$$\cos \phi = \frac{V_{\text{RMS}}^2}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}} \cdot \frac{R}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}}$$

$$= \frac{V_{\text{RMS}}^2 R}{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$



$$Q = \frac{\omega_0}{\Delta\omega}$$

$$Q = \frac{\omega_0 L}{R}$$



$$\omega_0 = \frac{1}{\sqrt{LC}}$$

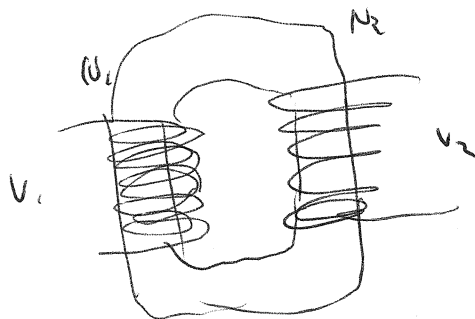
$$= \frac{1}{\sqrt{0.001 \text{ H} \times 10 \times 10^{-12} \text{ F}}} = \frac{1}{\sqrt{10^{-14}}}$$

for $\omega_0 = 10^7 \text{ rad/s}$

for $\omega_0 = 10^7 \text{ rad/s}$

$$Q = \frac{10^7 / 3 \times 10^{-3} \text{ H}}{100 \Omega} = \frac{10^4}{100} = \boxed{100}$$

TRANSFORMERS



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$$\Phi$$
$$V_2 = N_2 B_1 = -N_2 \frac{dB_1}{dt}$$

$$V_1 = -N_1 \frac{dB_1}{dt}$$

$$B_1 = \mu_0 \frac{N_1}{l_1} I_1$$

$$V_2 = -\mu_0 \frac{N_1 N_2}{l_1} \frac{dI_1}{dt}$$